

ENEE 460 Fall 2016 **Homework Set 6**: Assigned Wednesday October 12, 2016 - due back **at the start** of class on Wednesday, October 19, 2016

1. Read Chapter 6 on Linear Systems (2nd edition of book) – section 6.4 on Linearization, and how it comes in handy in solving stability problems as illustrated in section 5.3 of Chapter 5 on Dynamic Behavior. Read Chapter 5, sections 5.1 – 5.3 inclusive.

2. Do Problem
6.10

3. Consider solution to problem 2(a) in mid-term 1, setting the constants a_1 , a_2 , b_2 all equal to 1, but **without** the small angle assumption or approximation. Write a MATLAB simulation with general control input u allowed. Now consider control input $u(t) = \sin(at + b)$, for a range of frequencies a and phase values b . Run the simulation and determine a suitable range of these parameters such that the pendulum is stabilized about the straight up equilibrium **in your numerical experiments**. Provide plots of your results and copies of your code. Clearly state your experimental results.

4. Consider the dynamics (5.6) obtained by perturbing a linear oscillator. First verify by simulation that Figure 5.5 is indeed the right behavior. Next, suggest a new version of equation 5.6 (**hint** – we are looking for a slightly different perturbation) so that the resulting numerical behavior is qualitatively the same as in Figure 5.5, but the trajectories tend toward a circle of radius 2.

5. Determine the linearization of the dynamics (5.6) around the equilibrium at $(0, 0)$. How well do the trajectories of the linearization correspond to the trajectories of the nonlinear system (5.6)?