

# **Application-Oriented Policies and their Composition**

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- **Systems and Applications**
- **Property Types; Dependencies**
- **Policy Structure**
- **Policy Composition**

# Systems

- *state machine*  
STATES, SUBJECTS, USERS, OPERATIONS, OBJECTS
- *state transitions*
  - commands:  $op(s_1, S, obj, s_2)$
  - command sequence:  $op_1(s_0, S_1, obj, s_1)op_2(s_1, S_2, obj_2, s_2)\dots$ ,
  - tranquil commands: do not alter security attributes
- *system*: a set of command sequences with start states  $s_0$  in STATES $_0$ .
- *secure state, commands*: those that satisfy properties
- *reachable state*: a state appearing in a command sequence of a system
- *secure system*: all state transitions and reachable states are secure
- $\Omega$  : set of all command sequences of a secure system

# Applications and Executability

- application:  $\text{App} = [\text{ObjSet}, \text{OpSet}, \text{Plan}]$ 
  - **plan: a finite set of pairs**  $\{(\text{obj}_i, \text{op}_i)\}$
  - ordered plan: an ordered set of pairs  $\{(\text{obj}_i, \text{op}_i)\}$
  - plans with “operation bracketing” (e.g., least-privilege princ.)
  -
- $\text{App}_1 \cup \text{App}_2 =$   
 $[\text{ObjSet}_1 \cup \text{ObjSet}_2, \text{OpSet}_1 \cup \text{OpSet}_2, \text{Plan}_1 \cup \text{Plan}_2]$
- command sequence  $\sigma$  *executes*  $\text{App}$  if for any pair  $(\text{obj}_i, \text{op}_i)$  in  $\text{Plan}$  there is a command  $\text{op}_i(s_k, S, \text{obj}_i, s_{k+1})$  in  $\sigma$

# Property Types

**P = Attribute (AT) properties  $\wedge$**

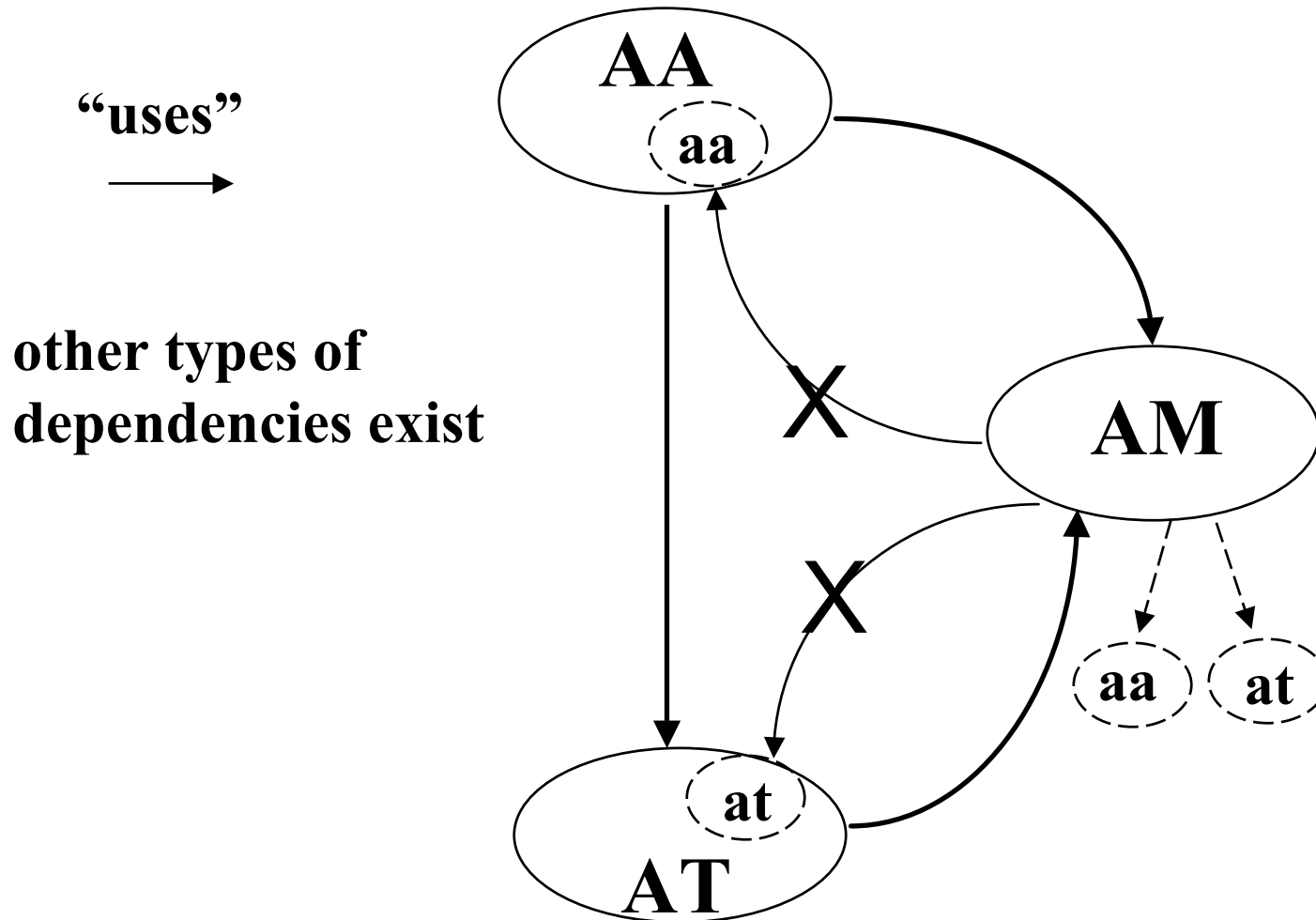
**Access Management (AM) properties  $\wedge$**

**Access Authorization (AA) properties**

# Examples of Property Types

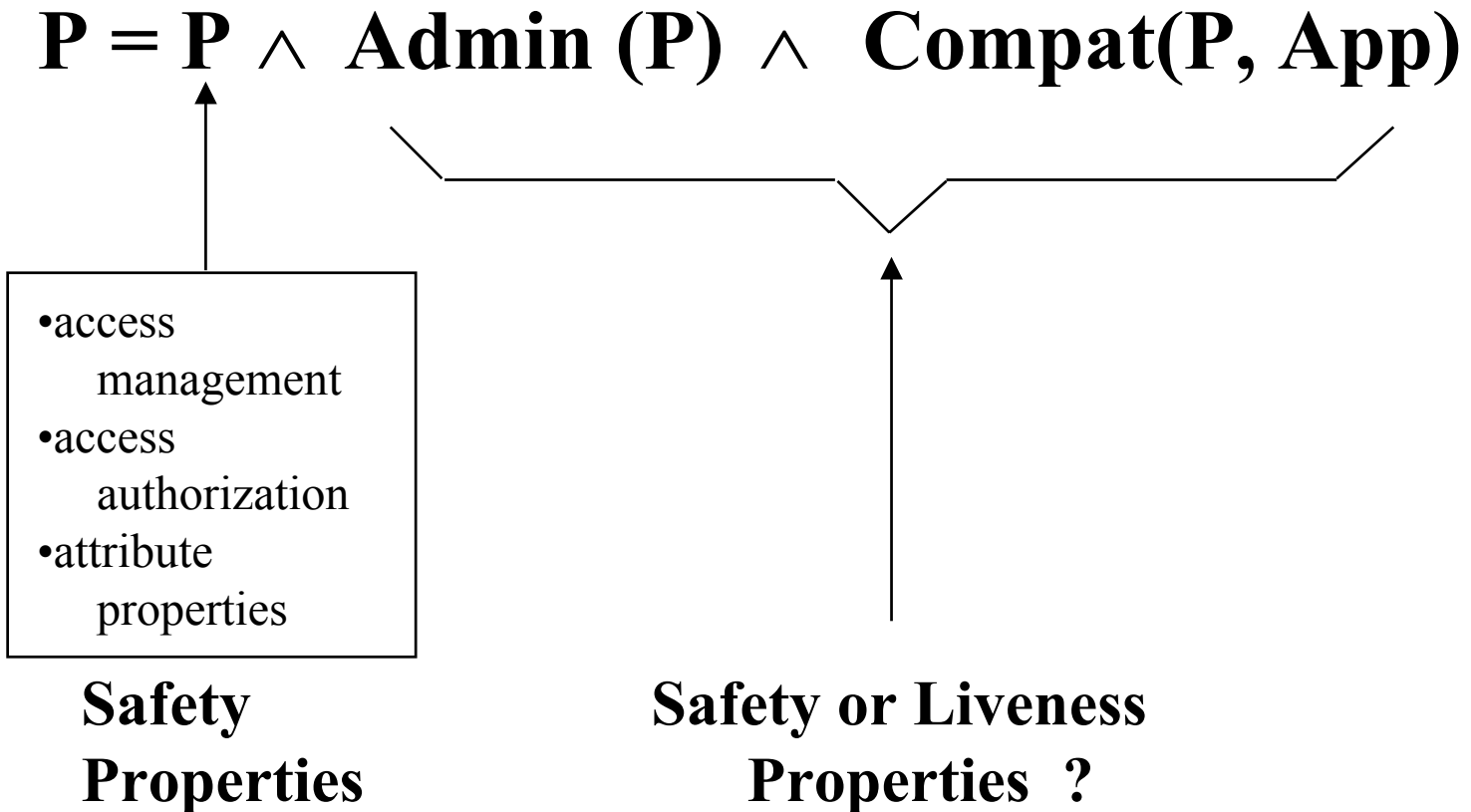
- **Attribute (AT) Properties**
  - security (integrity) levels, partial order, lattice property
  - roles, hierarchy, permissions, membership, inheritance
- **Access Management (AM) Properties**
  - distribution, review, revocation of permissions
    - selectivity, transitivity, independence ...
  - object / subject creation and destruction
  - object encapsulation
- **Access Authorization (AA) Properties**
  - required subject and object attributes for access
    - BLP, Biba, RBAC, UNIX ...

# Property Dependencies



**Individual policy properties cannot be composed independently**

# Policy Structure



# Admin(P)

P: a set of tranquil command sequences with the start state in  $STATES_0$

*for all*

$Admin(P) =$  “for each  $s$  in  $STATES$ , *there exists*  $s_0 \in STATES_0$ ,  
there exists  $\omega \in \Omega$  such that:  $\omega$  starts in  $s$ , and  
 $\omega$  reaches  $s_0$  and  
 $s_0^*$  is in P”

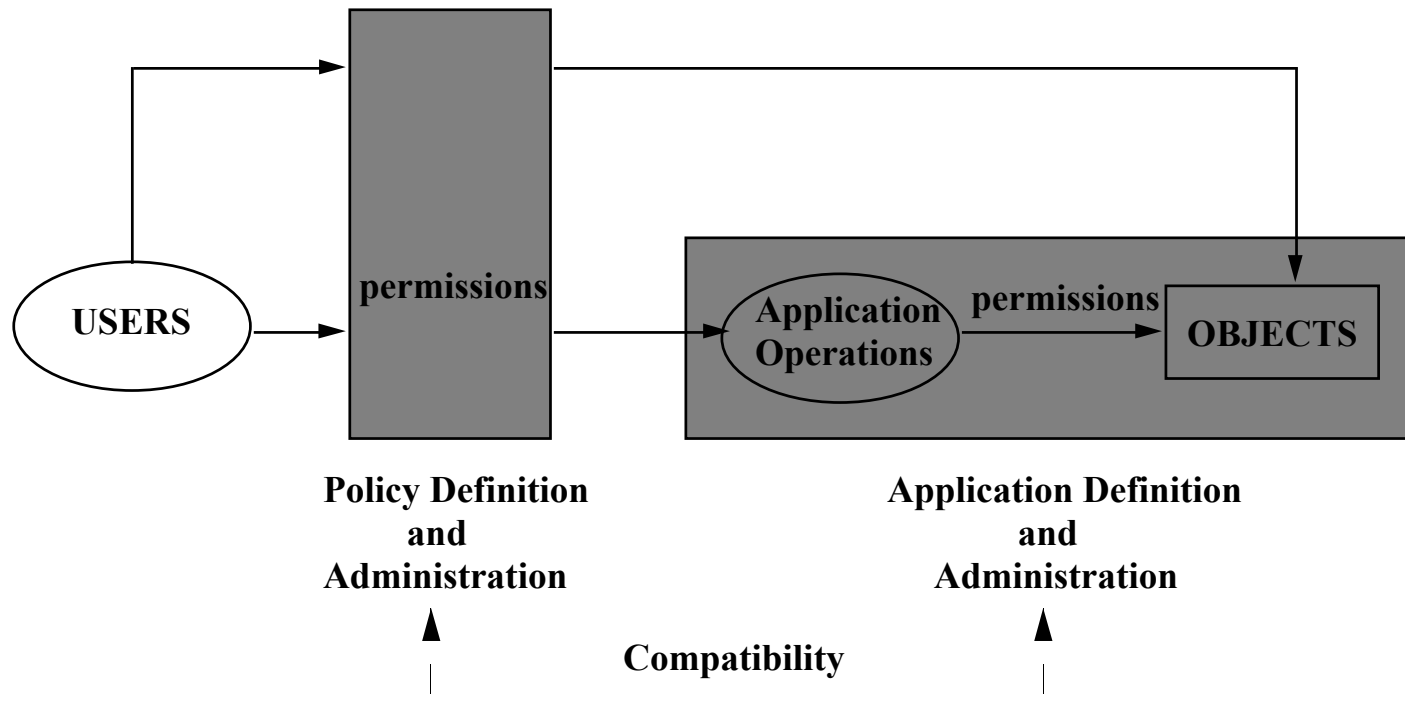
# Compat(P, App)

$Compat(P) =$  “there exists  $s_0 \in STATES_0$  and  $\sigma \in P$  starting in  $s_0$   
such that  $\sigma$  executes App”

**.... neither Safety nor Liveness ....**

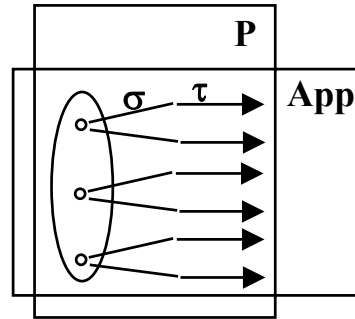


# Mandated Compatibility

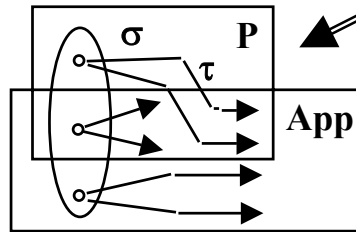


# Types of Compatibility

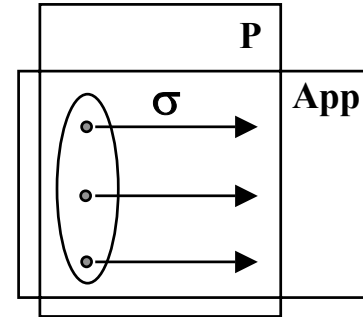
*Safety-Liveness Framework*



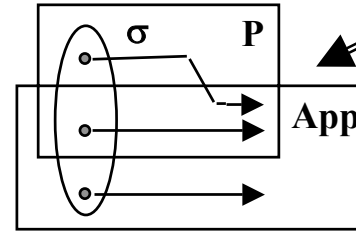
**Totally multi-path  
Compatible**



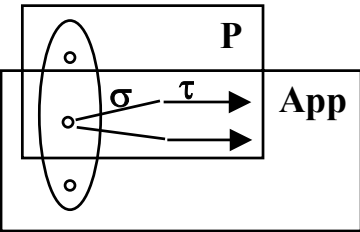
**Machine Closed  
Compatible**



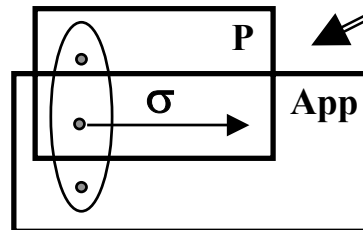
**Totally  
Compatible**



**Strongly  
Compatible**



**Multi-path  
Compatible**



**Compat(P, App)**

### **Totally Multi-path Compatible**

For each start state  $s_0$  there is a command sequence  $\sigma$  in  $P$  starting in  $s_0$ , and for each finite command sequence  $\sigma$  in  $P$  there is a command sequence  $\tau$  such that  $\sigma\tau$  is in  $P$  and executes *App*.

### **Machine-Closed Compatible**

For each finite command sequence  $\sigma$  in  $P$  there is a command sequence  $\tau$  such that  $\sigma\tau$  is in  $P$  and executes *App*.

### **Multi-path Compatible**

There is a start state  $s_0$  such that for each finite command sequence  $\sigma$  in  $P$  starting in  $s_0$  there is  $\tau$  such that  $\sigma\tau$  is in  $P$  and executes *App*.

### **Totally Compatible**

For each start state  $s_0$  there is a command sequence  $\sigma$  in  $P$  starting in  $s_0$  such that  $\sigma$  executes *App*.

### **Strongly Compatible**

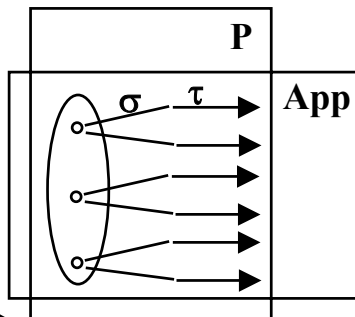
For each start state  $s_0$  such that  $s_0^*$  is in  $P$ , there is a command sequence  $\sigma$  in  $P$  starting in  $s_0$  that executes *App*.

### **Compatible**

There is a start state  $s_0$  and a command sequence  $\sigma$  in  $P$  starting in  $s_0$  that executes *App*.

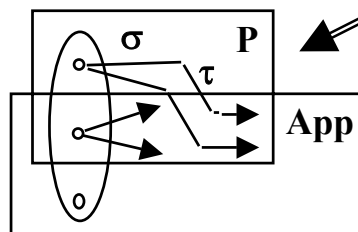
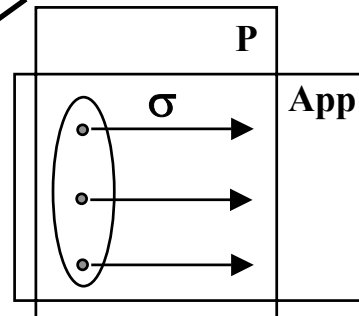
# Types of Compatibility

*Overly Restrictive*  
STATES<sub>0</sub>



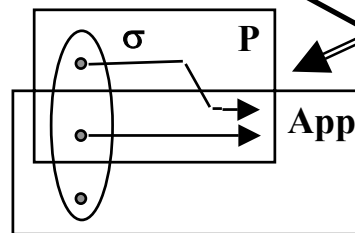
*Overly Restrictive* σs

Totally multi-path  
Compatible



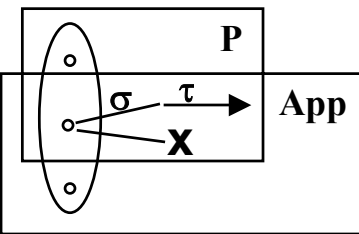
Machine-Closed  
Compatible

Totally  
Compatible

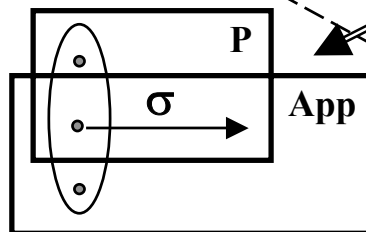


Strongly  
Compatible

*May Require Administrative  
Work for App's Execution in P*



Multi-path  
Compatible



**Compat(P, App)**

# Overly Restrictive $\sigma_s$

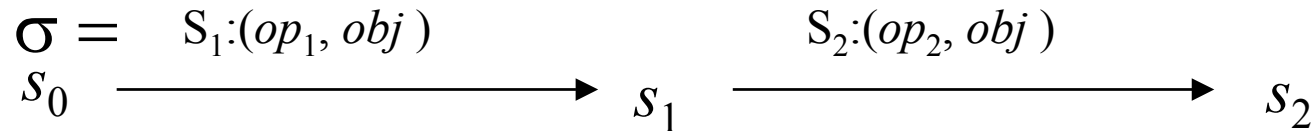
**Example:**

$App = [ \{obj\}, \{op_1, op_2\}, plan ]$ ;  $plan = \{(obj, op_1), (obj, op_2)\}$

$P$  : “ $u_1$  and  $u_2$  are the only users who may execute  $App$  and

a user may not execute two distinct operations on the same object”

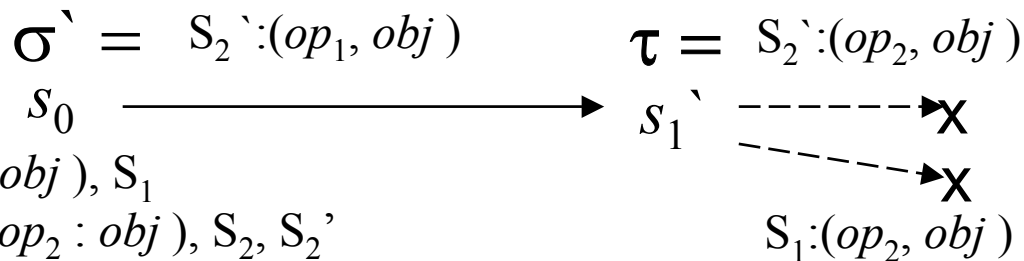
**Compat(P, App) is true**



$u_1: (op_1: obj), S_1 = \text{subject}$

$u_2: (op_1, op_2: obj), S_2, S_2' = \text{subjects}$

**Compat<sub>M</sub>(P, App) is false**



$u_1: (op_1: obj), S_1$

$u_2: (op_1, op_2: obj), S_2, S_2'$

# Policy Composition

$$\mathbf{P}_1 = \mathbf{P}_1 \wedge \text{Admin}(\mathbf{P}_1) \wedge \text{Compat}(\mathbf{P}_1, \text{App}_1)$$

$$\mathbf{P}_2 = \mathbf{P}_2 \wedge \text{Admin}(\mathbf{P}_2) \wedge \text{Compat}(\mathbf{P}_2, \text{App}_2)$$

Let  $\text{CS}(\mathbf{P}_1)$ ,  $\text{CS}(\mathbf{P}_2)$  denote sets of command sequences

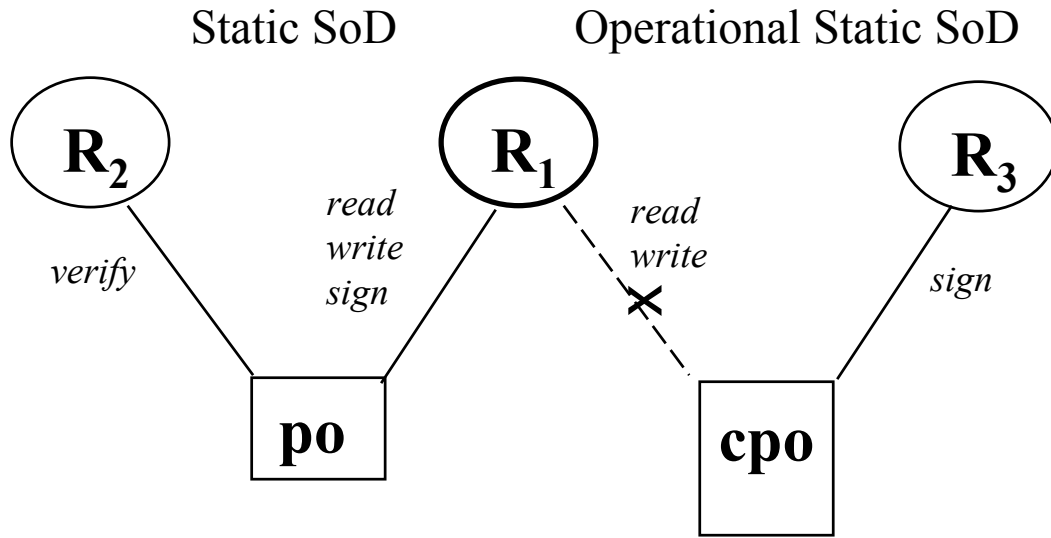
$\mathbf{P}_1$ ,  $\mathbf{P}_2$  are composable if and only if

$$\text{CS}(\mathbf{P}_1 \cap \mathbf{P}_2) \neq \emptyset \text{ whenever } \text{CS}(\mathbf{P}_1), \text{CS}(\mathbf{P}_2) \neq \emptyset$$

*Emerging policy*  $\mathbf{P}_1 \circ \mathbf{P}_2 =$

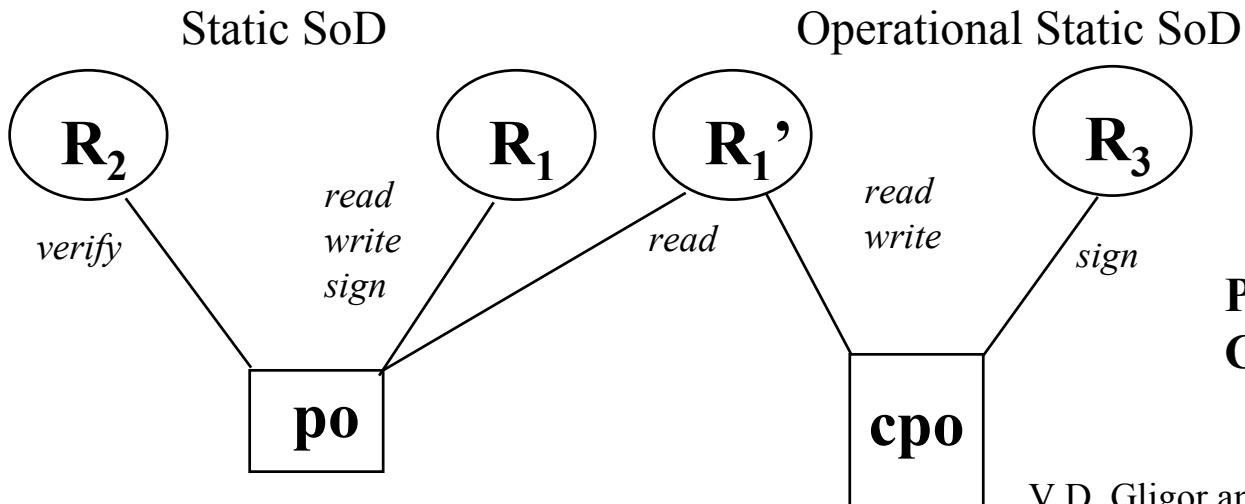
$$= \mathbf{P}_1 \wedge \mathbf{P}_2 \wedge \text{Admin}(\mathbf{P}_1 \wedge \mathbf{P}_2) \wedge \text{Compat}(\mathbf{P}_1 \wedge \mathbf{P}_2, \text{App}_1 \cup \text{App}_2)$$

# Example: Non-Composable Separation-of-Duty Policies



**Purchasing Staff  
Department**

**Purchasing Staff  
Central Administration**



**Policy-Management  
Change**