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Authentication: Theory and Practice, Taos OS

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Logic (1)

1. **K says S**

$(A \text{ and } B) \text{ says } S \equiv (A \text{ says } S) \text{ and } (B \text{ says } S)$

if $A = B$, then $(A \text{ says } S) \equiv (B \text{ says } S)$

Example of use:

- signatures $\langle S, \{S\}^K \rangle$

- request transmission on a channel: **C says RQ**

2. $A \Rightarrow B$ (**A speaks for B**)

$(A \Rightarrow B) \equiv (A = A \text{ and } B)$

if $A \Rightarrow B$ and $(A \text{ says } S)$, then $(B \text{ says } S)$

\Rightarrow is a partial order (i.e., is reflexive, antisymmetric, transitive)

Example of use:

- unsigned certificates: $\langle A, K \rangle \equiv K$ is A's public key

- group membership: $A \Rightarrow G \equiv A$ is a member of G

o groups cannot speak; they have neither channels nor keys

Logic (2)

3. $B \mid A$ (**B quoting A**)

($B \mid A$ **says S**) \equiv (**B says A says S**)

Example of use:

- $K_b \mid K_a$ **says S** $\equiv \{S\}^{K_a} \rightarrow S \rightarrow \{S\}^{K_b}$
S went through a relay

4. **B for A**

if **B for A**, then(**B says A says S**) and **A delegated to B**

A says ((B | A) \Rightarrow (B for A))

Note: (**B for A**) is stronger than ($B \mid A$)

Example of use:

- delegation certificates; e.g., login certificates

Logic (3)

5. A as R (A in role R)

if (A as R) says S, then (A says R says S)

A as R = A | R only if R = **role**

A \Rightarrow A as R only if R = **role** (A $\neq \Rightarrow$ A | R for any R)

Example of use:

- booting certificates
- restricting user privileges

6. Delegation Axiom

if A says ((B | A) \Rightarrow (B for A)), then ((B | A) \Rightarrow (B for A))

Note: This axiom does **not** require B to accept delegation; i.e.,

(B | A) says ((B | A) \Rightarrow (B for A))

Logic (4)

7. Hand-off Axiom

if (A **says** (B \Rightarrow A)), then B \Rightarrow A

8. Inter-realm Certificate Validation Axioms

(1) P **except** M \Rightarrow P

(2) if M \neq N, then ((P **except** M) | N) \Rightarrow P / N **except** “..”

(3) if M \neq “..”, then (P / N **except** M | “..”) \Rightarrow P **except** N

9. Theorems

(1) Monotonicity of **and**, |, **for**, and **as** w.r.t. \Rightarrow

if A \Rightarrow B then (A **and** C \Rightarrow B **and** C)

A | C \Rightarrow B | C

A **for** C \Rightarrow B **for** C

A **as** C \Rightarrow B **as** C

Logic (5)

(1) Monotonicity of **and**, **|**, **for**, and **as** w.r.t. \Rightarrow

if $(A \Rightarrow B \text{ and } C \Rightarrow C')$ then $(A \text{ and } C \Rightarrow B \text{ and } C')$

$A | C \Rightarrow B | C'$

$A \text{ for } C \Rightarrow B \text{ for } C'$

$A \text{ as } C \Rightarrow B \text{ as } C'$

(2) Transitivity of \Rightarrow

if $A \Rightarrow B$ **and** $B \Rightarrow C$, then $A \Rightarrow C$

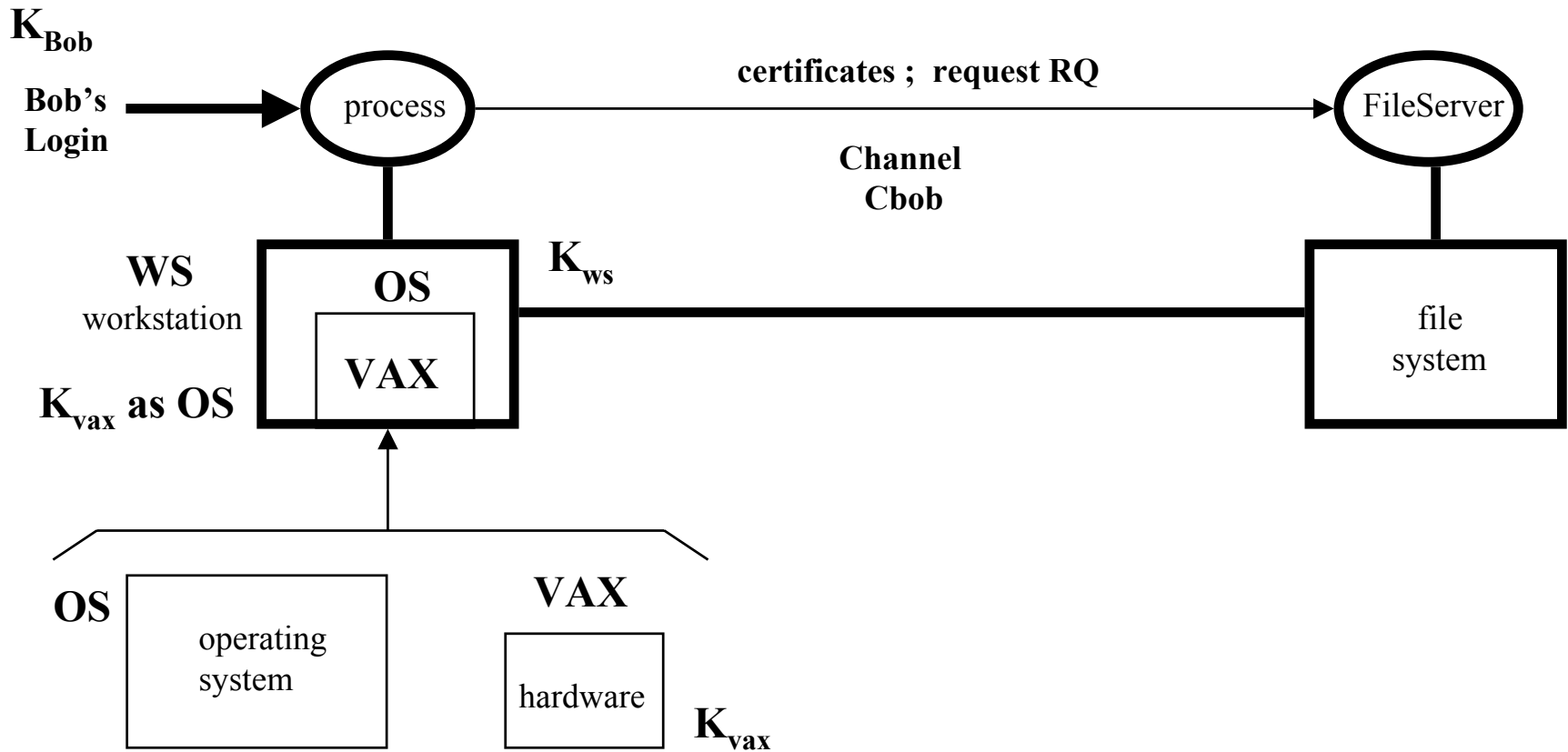
(3) Hand-off Rule

if $(A' \Rightarrow A)$ **and** A' **says** $(B \Rightarrow A)$, then $B \Rightarrow A$

(4) Joint Authority Rule (Revocation; Limited-Time Login)

if $((A' \text{ and } B) \Rightarrow A)$ **and** $(B \Rightarrow A')$, then $B \Rightarrow A$

Authenticating a Remote Request



RQ Authentication: Was RQ received on Channel Cbob issued by Bob after login to workstation WS (which was obtained by booting OS on VAX) ?

RQ Authentication: File Server wants to establish (*VAX as OS*) for Bob says RQ

File Server wants to establish (*VAX as OS*) *for Bob says RQ*

File Server needs:

- (1) axioms and theorems of the logic
- (2) certificates it receives or has
- (3) trust relationships established

Certificates:

- (1) booting : $(K_{\text{vax}} \text{ as OS }) \text{ says } (K_{\text{ws}} \Rightarrow K_{\text{vax}} \text{ as OS })$
- (2) login: $K_{\text{Bob}} \text{ says } (K_{\text{ws}} \mid K_{\text{Bob}}) \Rightarrow (K_{\text{ws}} \text{ for } K_{\text{Bob}})$
- (3) channel: $(K_{\text{ws}} \mid K_{\text{Bob}}) \text{ says } (C_{\text{Bob}} \Rightarrow (K_{\text{ws}} \text{ for } K_{\text{Bob}}))$
(authority hand-off)
- (4) VAX: $K_{\text{ca}} \text{ says } K_{\text{vax}} \Rightarrow \text{VAX}$
- (5) Bob: $K_{\text{ca}} \text{ says } K_{\text{Bob}} \Rightarrow \text{Bob}$

Trust Relationship

any principal trusts: $K_{\text{ca}} \Rightarrow \text{principal}$

File Server's Logic (1)

by Delegation axiom (applied to **login** certificate)

$$(1) (K_{ws} \mid K_{Bob}) \Rightarrow (K_{ws} \text{ for } K_{Bob})$$

by \Rightarrow (applied to channel certificate $(K_{ws} \mid K_{Bob})$ **says** $(C_{Bob} \Rightarrow (K_{ws} \text{ for } K_{Bob}))$ and (1))

$$(2) (K_{ws} \text{ for } K_{Bob}) \text{ says } (C_{Bob} \Rightarrow (K_{ws} \text{ for } K_{Bob}))$$

by Hand-off axiom (applied to (2))

$$(3) C_{Bob} \Rightarrow (K_{ws} \text{ for } K_{Bob})$$

by \Rightarrow (applied to incoming request, namely, C_{Bob} **says** RQ and (3))

$$(4) (K_{ws} \text{ for } K_{Bob}) \text{ says } RQ$$

by Hand-off axiom (applied to **booting** certificate))

$$(5) K_{ws} \Rightarrow (K_{vax} \text{ as OS})$$

File Server's Logic (2)

by monotonicity of **for** (applied to (5))

(6) $K_{ws} \text{ for } K_{Bob} \Rightarrow (K_{vax} \text{ as OS }) \text{ for } K_{Bob}$

by \Rightarrow (applied to (4) and (6))

(7) $((K_{vax} \text{ as OS }) \text{ for } K_{Bob}) \text{ says RQ}$

by **trust** (to Bob and VAX)

(8) $K_{ca} \Rightarrow VAX$

(9) $K_{ca} \Rightarrow Bob$

by \Rightarrow (to (8), (9), Bob and Vax' certificates)

(10) $K_{vax} \Rightarrow VAX$

(11) $K_{Bob} \Rightarrow Bob$

by monotonicity of **as** (to (10))

(12) $(K_{vax} \text{ as OS }) \Rightarrow VAX \text{ as OS}$

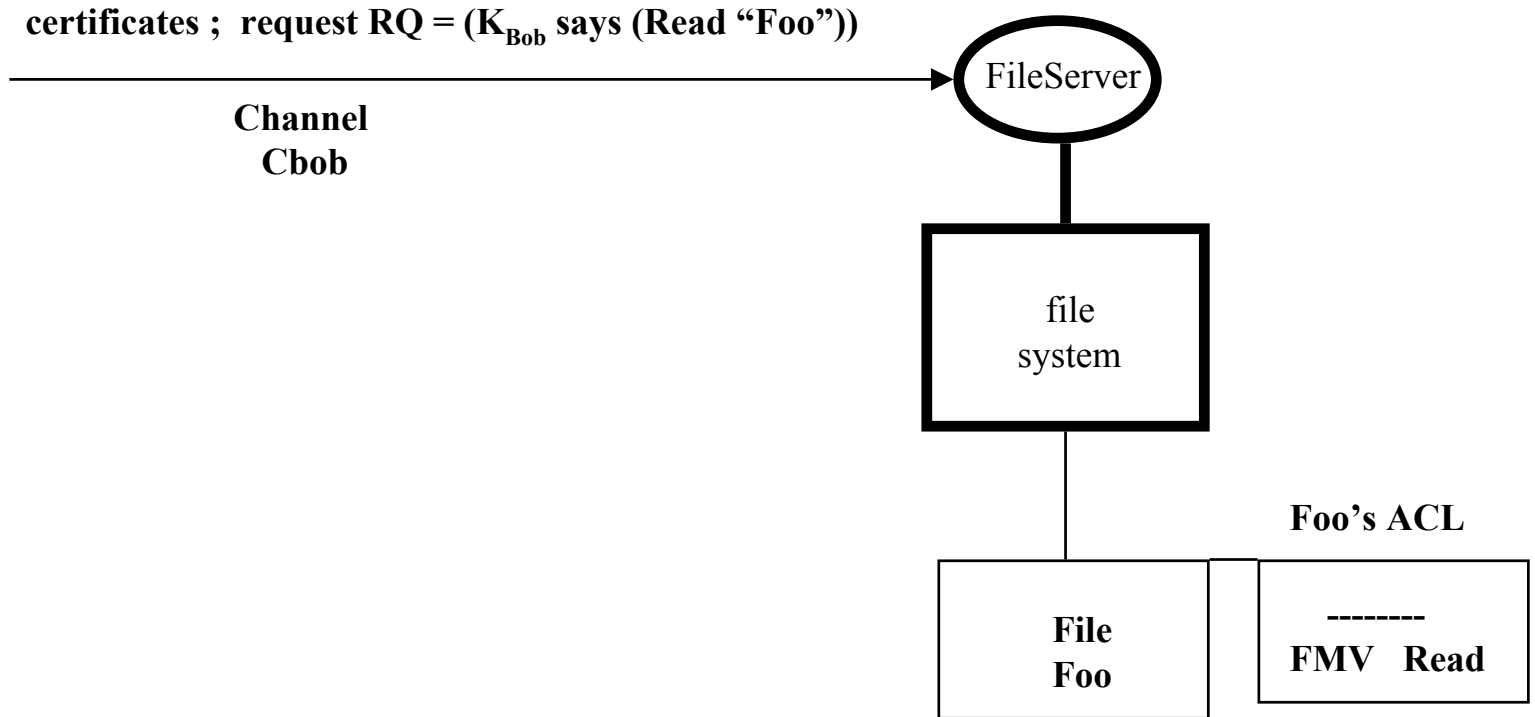
by monotonicity of **for** (to (11) and (12))

(13) $(K_{vax} \text{ as OS }) \text{ for } K_{Bob} \Rightarrow (VAX \text{ as OS}) \text{ for Bob}$

by \Rightarrow (to (7) and (13))

$(VAX \text{ as OS}) \text{ for Bob says RQ}$

Performing Access Control



RQ Access Control: Is Bob allowed Read access to File "Foo"?

RQ Access Control: File Server wants to establish that Bob's $RQ = FMV \text{ says } (\text{Read "Foo"})$ and that FMV is authorized to Read "Foo" by searching Foo's ACL

File Server's Logic (3)

Additional Certificates:

(6) Group: K_{ca} **says** Bob \Rightarrow FMV

by trust,

(14) $K_{ca} \Rightarrow$ FMV

by \Rightarrow (applied to **Group** certificate (6) and (14))

(15) FMV **says** Bob \Rightarrow FMV

by Hand-off Axiom (applied to (15))

(16) Bob \Rightarrow FMV

by \Rightarrow (applied to (11) and request $RQ = (K_{Bob}$ **says** (Read "Foo"))

(17) Bob **says** (Read "Foo")

by \Rightarrow (applied to (16) and (17))

FMV **says** (Read "Foo")

Validation of Interrealm Certificates (in DSSA)

B wants to establish $K_F \Rightarrow /D/F$ **except** “..”

B needs to use:

- (1) available certificates
- (2) trust relationships
- (3) axioms and theorems

Certificates :

K_B | ‘..’ **says** [$K_C \Rightarrow (/C$ **except** $B)$]

K_C | ‘..’ **says** [$K_{root} \Rightarrow (/$ **except** $C)$]

K_{root} | D **says** [$K_D \Rightarrow (/D$ **except** ‘..’)]

K_D | F **says** [$K_F \Rightarrow (/D/F$ **except** ‘..’)]

Trust Relationships

everyone trusts its key; e.g., **B** trusts ($K_B \Rightarrow /C/B$ **except** *nil*)

B's Logic (1)

by trust

(1) **B trusts** $K_B \Rightarrow /C/B \text{ except } nil$

by interrealm Axiom (3) (applied to B)

(2) $((/C/B \text{ except } nil) \mid '..')$ $\Rightarrow (/C \text{ except } B)$

by monotonicity of \mid w.r.t \Rightarrow (applied to 1)

(3) $K_B \mid '..' \Rightarrow ((/C/B \text{ except } nil) \mid '..')$

by transitivity of \Rightarrow

(4) $K_B \mid '..' \Rightarrow /C/B \text{ except } B$

by using certificate

$K_B \mid '..' \text{ says } [K_C \Rightarrow (/C \text{ except } B)]$ and the Hand-off Theorem

(5) $K_C \Rightarrow /C \text{ except } B$

B's Logic (2)

(5) $K_C \Rightarrow /C \text{ except } B$

by interrealm Axiom (3) (applied to C)

(6) $((/C \text{ except } B) \mid \text{'..'}) \Rightarrow (/ \text{ except } C)$

by monotonicity of \mid w.r.t \Rightarrow (applied to 6)

(7) $K_C \mid \text{'..'} \Rightarrow ((/C \text{ except } B) \mid \text{'..'})$

by transitivity of \Rightarrow

(8) $K_C \mid \text{'..'} \Rightarrow / \text{ except } C$

by using certificate

$K_C \mid \text{'..'} \text{ says } [K_{\text{root}} \Rightarrow (/ \text{ except } C)]$ and the Handoff Theorem

(9) $K_{\text{root}} \Rightarrow / \text{ except } C$

B's Logic (3)

(10) $K_{\text{root}} \Rightarrow / \text{except } C$

by interrealm Axiom (2) (applied to *root*)

(11) $((/ \text{except } C) | D) \Rightarrow (/D \text{ except } \text{'..'})$

by monotonicity of $|$ w.r.t \Rightarrow (applied to 10)

(12) $K_{\text{root}} | D \Rightarrow ((/ \text{except } C) | D)$

by transitivity of \Rightarrow

(13) $K_{\text{root}} | D \Rightarrow /D \text{ except } \text{'..'}$

by using certificate

$K_{\text{root}} | D \text{ says } [K_D \Rightarrow (/D \text{ except } \text{'..'})]$ and the Handoff Theorem

(14) $K_D \Rightarrow /D \text{ except } \text{'..'}$

B's Logic (4)

(15) $K_D \Rightarrow /D \text{ except } \text{'..'}'$

by interrealm Axiom (2) (applied to D)

(16) $((D/ \text{ except } \text{'..'}) | F) \Rightarrow (/D/F \text{ except } \text{'..'})$

by monotonicity of $|$ w.r.t \Rightarrow (applied to 15)

(17) $K_D | F \Rightarrow ((/D \text{ except } \text{'..'}) | F)$

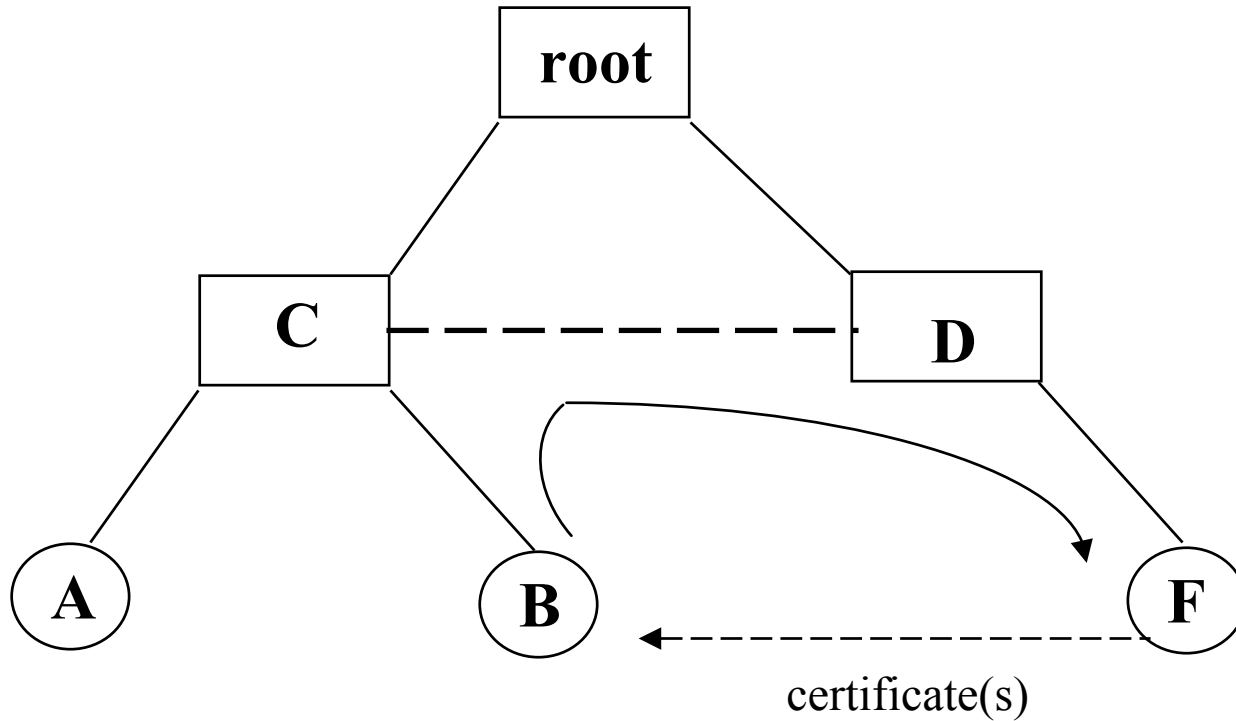
by transitivity of \Rightarrow

(19) $K_D | F \Rightarrow /D/F \text{ except } \text{'..'}'$

by using certificate

$K_D | F \text{ says } [K_F \Rightarrow (/D/F \text{ except } \text{'..'})]$ and the Handoff Theorem

(19) $K_F \Rightarrow /D/F \text{ except } \text{'..'}'$



B wants to establish $K_F \Rightarrow /D/F$ except “..”

Least Common Ancestor (B, F) = Link (C, D)
(in general, link \Rightarrow lca is no longer unique)