

On the Formal Definition of Separation-of-Duty (SoD) Policies and their Composition

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SoD premise:

- Violations that require collusion are less likely to happen

SoD goals:

- Separate sensitive tasks of an application such that integrity violations => collusion
- Minimize risk of collusion
by *careful* assignment of users to separate tasks

SoD implementation:

- Define integrity property of an application
- Partition application into separate operations and objects
- *carefully* assign of users to separate application partitions

SoD Policies

Advantage:

- **wide-spread acceptance by business, industry, government**

Drawbacks:

- *application-oriented policy*
 - => limited scope
 - => separate administration
- *family of policies*
 - => required system flexibility
- *uncertain policy interpretation*
 - => uncertain relative strength

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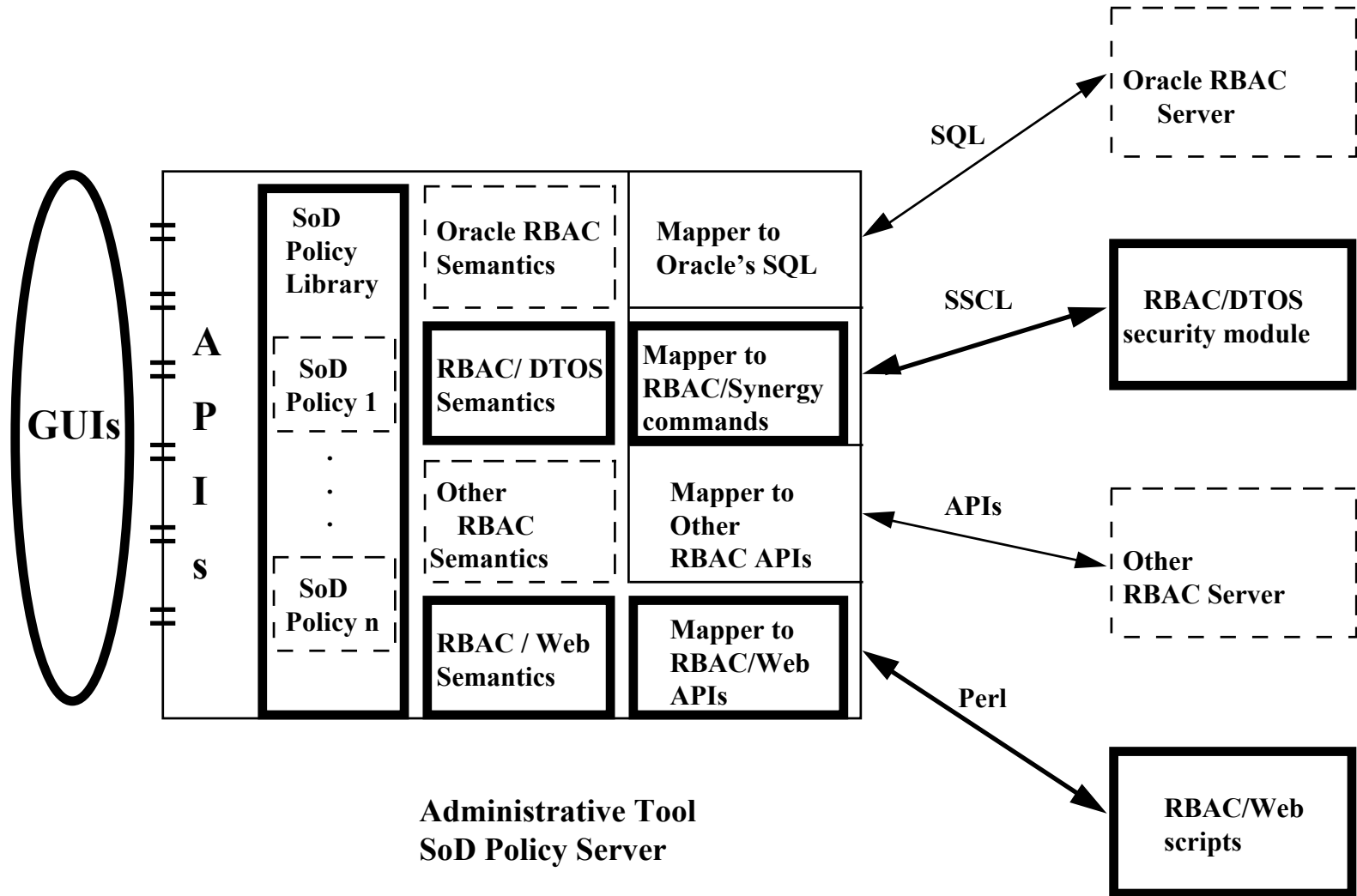
Mitigation:

- *make it a feature of a global policy*
- *provide administrative tools*
- *define formally*

Solution: Define, implement, and administer SoD policies in systems supporting Role-Based Access Control (RBAC)

{ users } → { roles } : { operations } → { objects }

Vision: SoD Administrative Tool



Systems

- *state machine*
STATES, SUBJECTS, USERS, OPERATIONS, OBJECTS
- *state transitions*
 - commands: $op(s_1, S, obj, s_2)$
 - command sequence: $op_1(s_0, S_1, obj, s_1)op_2(s_1, S_2, obj_2, s_2)\dots$,
 - tranquil commands: do not alter security attributes
- *system*: a set of command sequences with start states s_0 in STATES₀.
- *secure state, commands*: those that satisfy properties
- *reachable state*: a state appearing in a command sequence of a system
- *secure system*: all state transitions and reachable states are secure
- Ω : set of all command sequences of a secure system

Applications and Executability

- application: $\text{App} = [\text{ObjSet}, \text{OpSet}, \text{Plan}]$
 - **plan: a finite set of pairs** $\{(\text{obj}_i, \text{op}_i)\}$
 - ordered plan: an ordered set of pairs $\{(\text{obj}_i, \text{op}_i)\}$
 - plans with “operation bracketing” (e.g., least-privilege princ.)
 - ...
- $\text{App}_1 \cup \text{App}_2 =$
 $[\text{ObjSet}_1 \cup \text{ObjSet}_2, \text{OpSet}_1 \cup \text{OpSet}_2, \text{Plan}_1 \cup \text{Plan}_2]$
- command sequence σ *executes* App if for any pair $(\text{obj}_i, \text{op}_i)$ in Plan there is a command $\text{op}_i(s_k, S, \text{obj}_i, s_{k+1})$ in σ

Property Types

P = Attribute (AT) properties \wedge

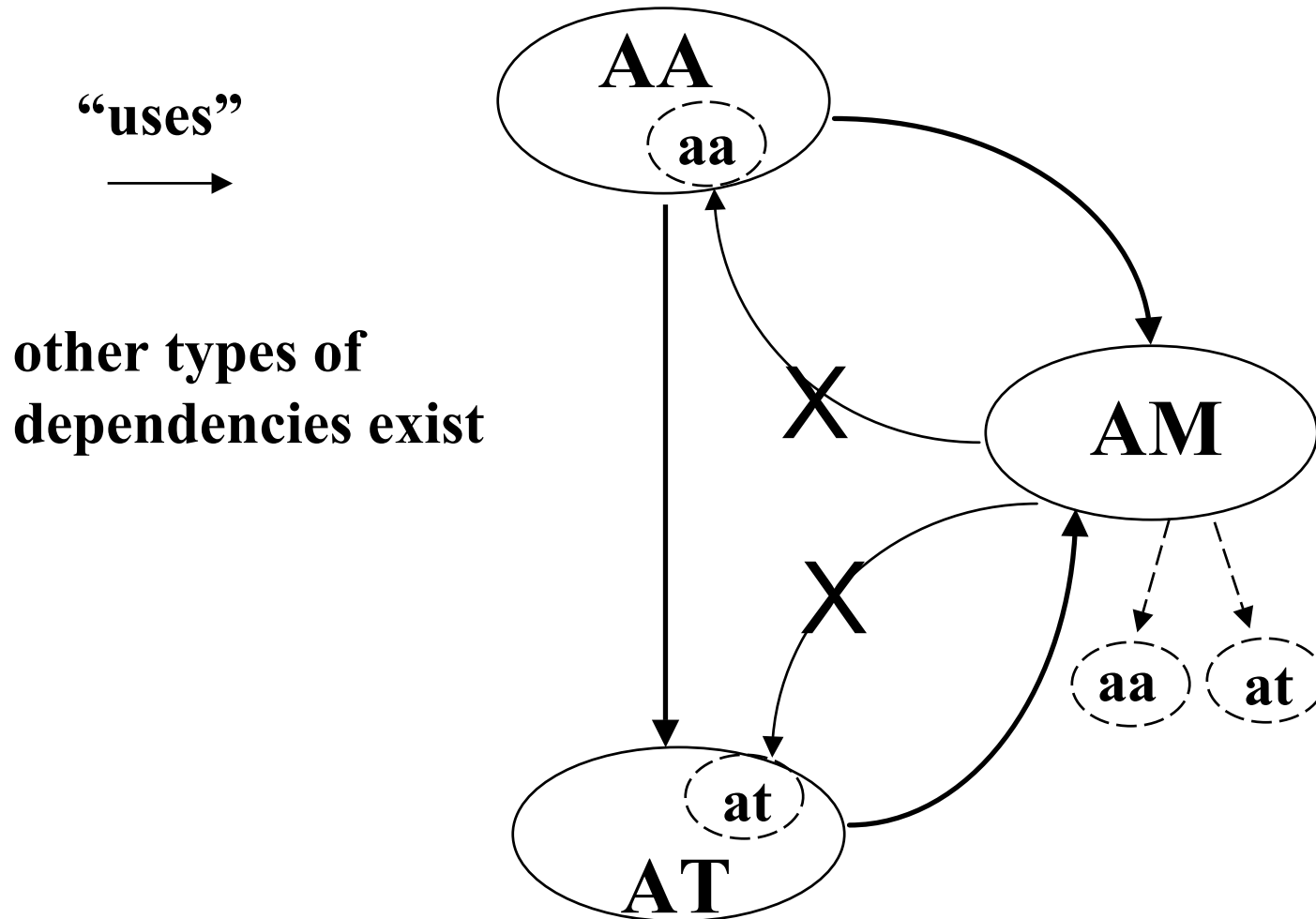
Access Management (AM) properties \wedge

Access Authorization (AA) properties

Examples of Property Types

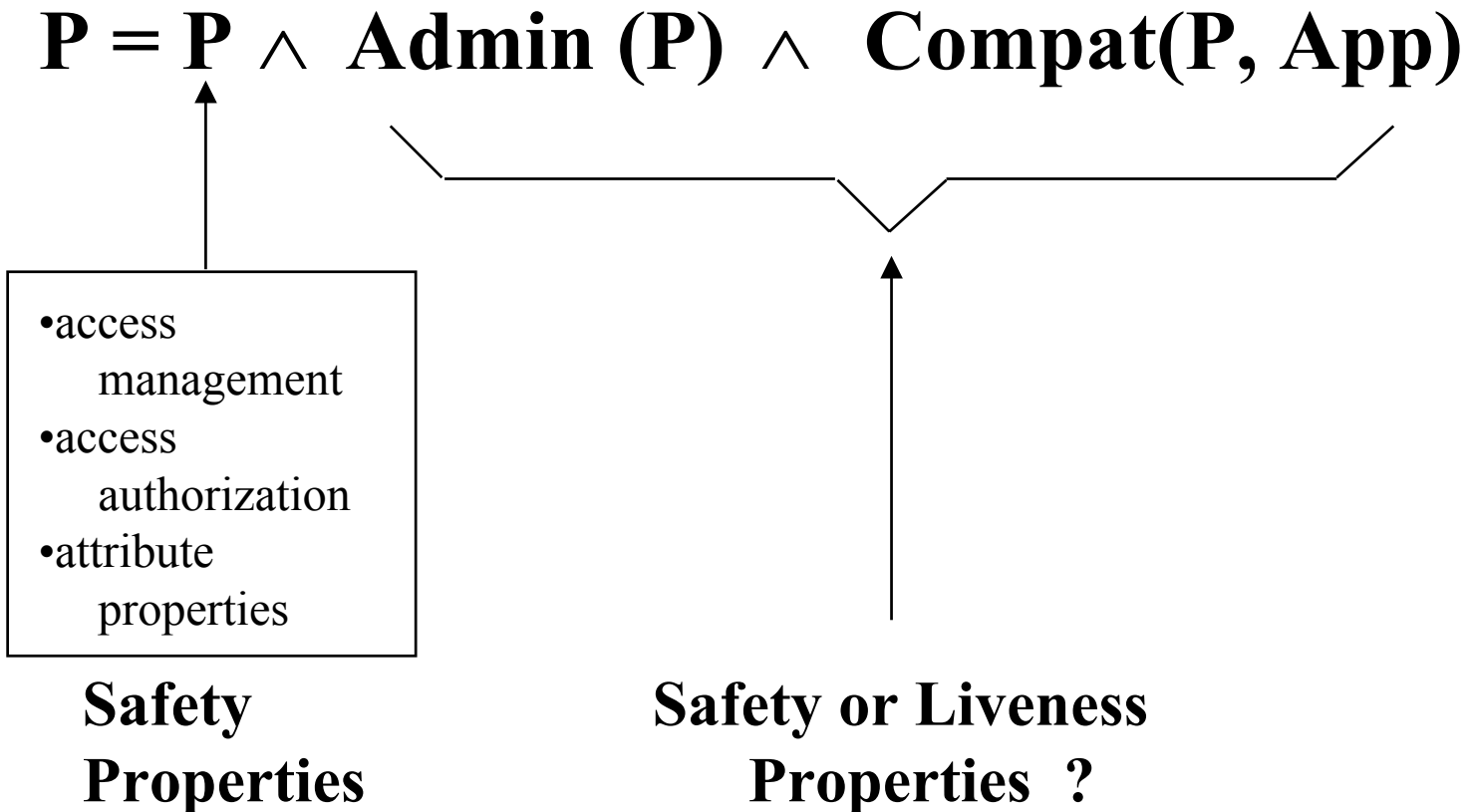
- **Attribute (AT) Properties**
 - security (integrity) levels, partial order, lattice property
 - roles, hierarchy, permissions, membership, inheritance
- **Access Management (AM) Properties**
 - distribution, review, revocation of permissions
 - selectivity, transitivity, independence ...
 - object / subject creation and destruction
 - object encapsulation
- **Access Authorization (AA) Properties**
 - required subject and object attributes for access
 - BLP, Biba, RBAC, UNIX ...

Property Dependencies



Individual policy properties cannot be composed independently

Policy Structure



SoD Policy Structure

$$\mathbf{SoD-P = SoD-P \wedge Admin(SoD-P) \wedge Compat(SoD-P, App) \wedge RBAC-P}$$

Admin(P)

P: a set of tranquil command sequences with the start state in $STATES_0$

for all

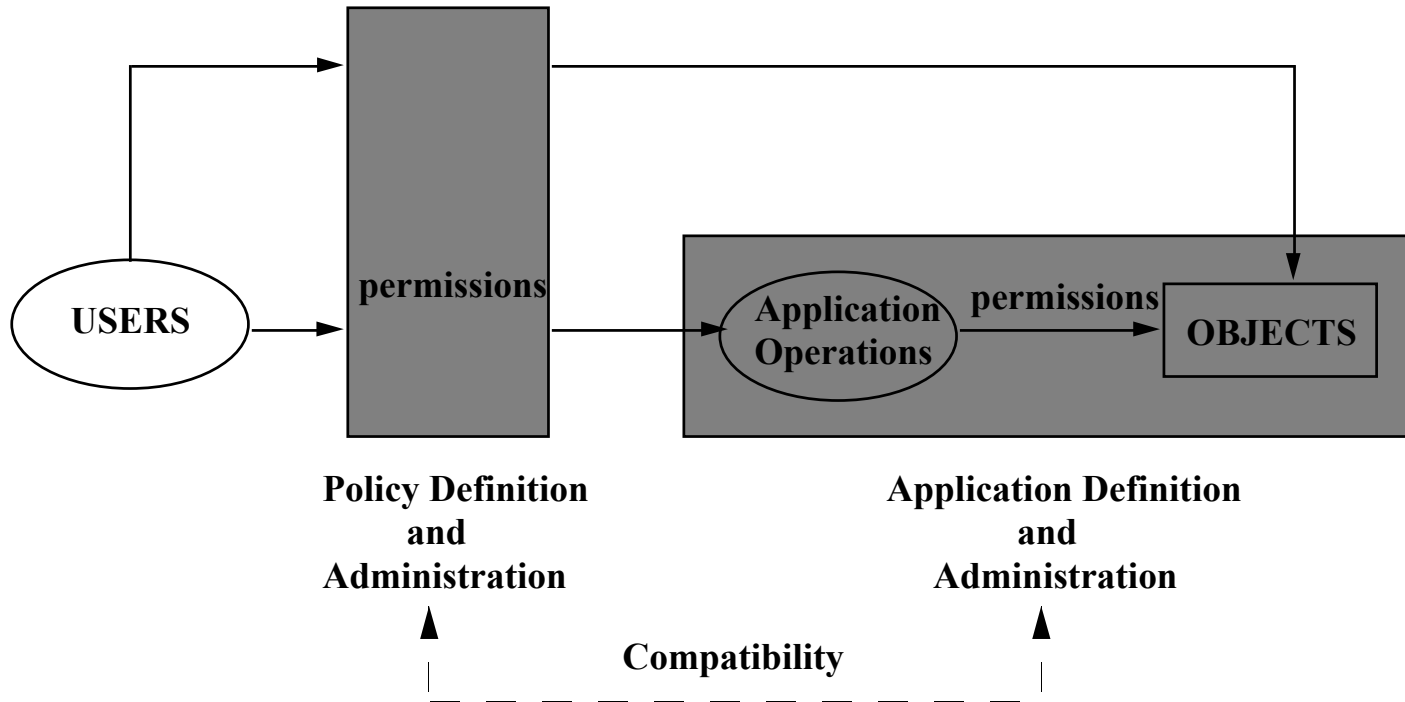
$Admin(P) =$ “for each s in $STATES$, *there exists* $s_0 \in STATES_0$,
there exists $\omega \in \Omega$ such that: ω starts in s , and
 ω reaches s_0 and
 s_0^* is in P”

Compat(P, App)

$Compat(P) =$ “there exists $s_0 \in STATES_0$ and $\sigma \in P$ starting in s_0
such that σ executes App”

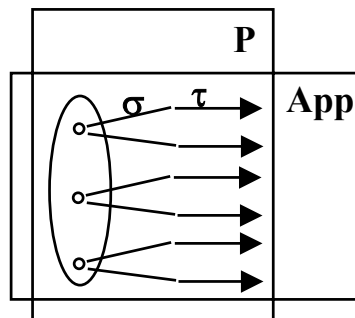
.... neither Safety nor Liveness

Mandated Compatibility

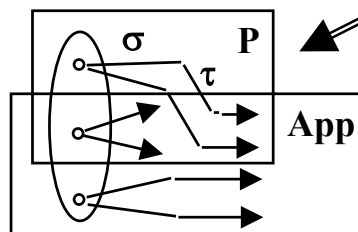


Types of Compatibility

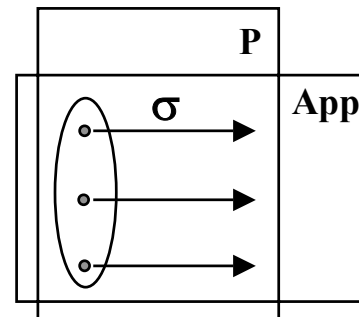
Safety-Liveness Framework



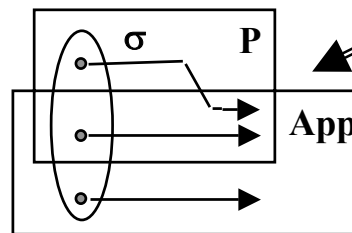
Totally multi-path Compatible



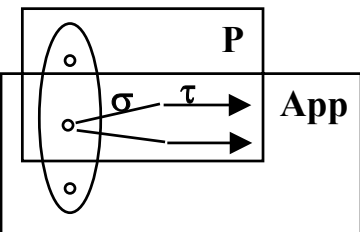
Machine Closed Compatible



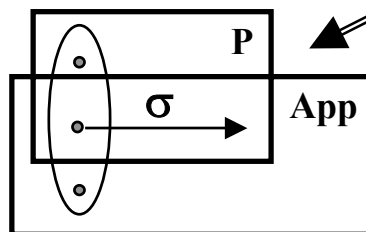
Totally Compatible



Strongly Compatible



Multi-path Compatible



Compat(P, App)

Totally Multi-path Compatible

For each start state s_0 there is a command sequence σ in P starting in s_0 , and for each finite command sequence σ in P there is a command sequence τ such that $\sigma\tau$ is in P and executes *App*.

Machine-Closed Compatible

For each finite command sequence σ in P there is a command sequence τ such that $\sigma\tau$ is in P and executes *App*.

Multi-path Compatible

There is a start state s_0 such that for each finite command sequence σ in P starting in s_0 there is τ such that $\sigma\tau$ is in P and executes *App*.

Totally Compatible

For each start state s_0 there is a command sequence σ in P starting in s_0 such that σ executes *App*.

Strongly Compatible

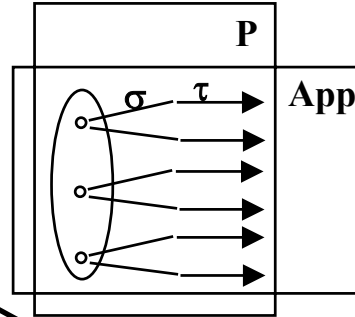
For each start state s_0 such that s_0^* is in P , there is a command sequence σ in P starting in s_0 that executes *App*.

Compatible

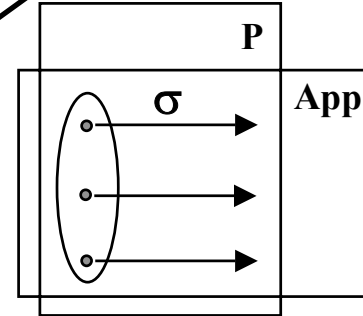
There is a start state s_0 and a command sequence σ in P starting in s_0 that executes *App*.

Types of Compatibility

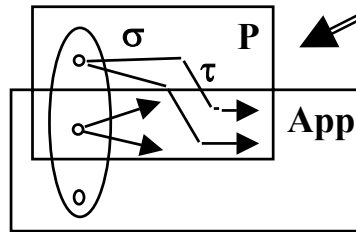
Overly Restrictive
STATES₀



Overly Restrictive σ s

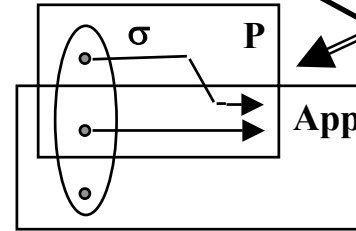


Totally multi-path
Compatible



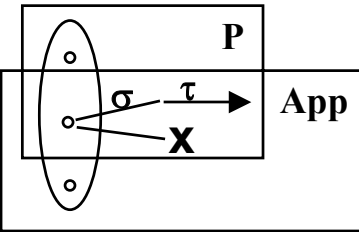
Machine-Closed
Compatible

Totally
Compatible

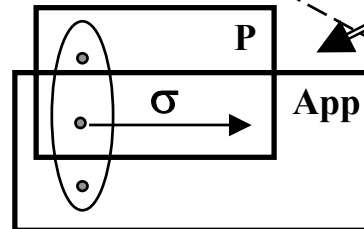


Strongly
Compatible

*May Require Administrative
Work for App's Execution in P*



Multi-path
Compatible



Compat(P, App)

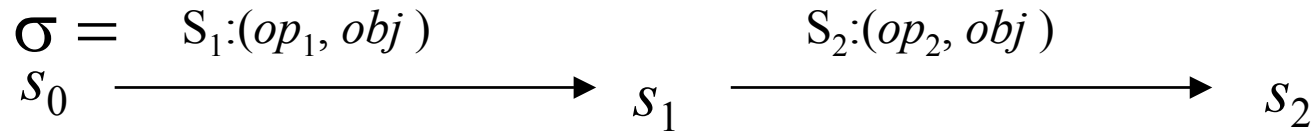
Overly Restrictive σ_s

Example:

$App = [\{obj\}, \{op_1, op_2\}, plan]; plan = \{(obj, op_1), (obj, op_2)\}$

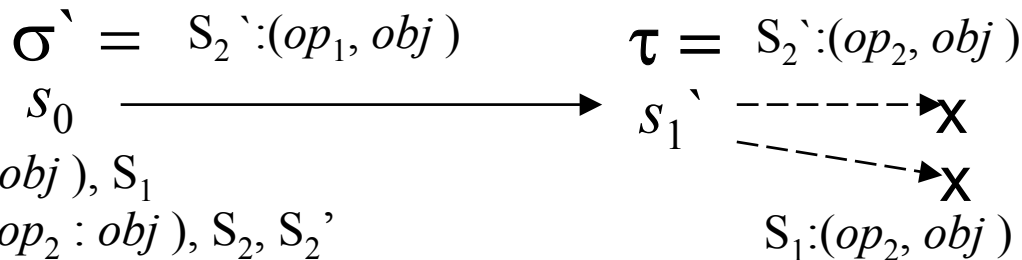
P : “ u_1 and u_2 are the only users who may execute App and a user may not execute two distinct (or all) operations on the same object”

Compat(P, App) is true



$u_1: (op_1: obj), S_1 = \text{subject}$
 $u_2: (op_1, op_2: obj), S_2, S_2' = \text{subjects}$

Compat_M(P, App) is false



$u_1: (op_1: obj), S_1$
 $u_2: (op_1, op_2: obj), S_2, S_2'$

Simple Policy Composition

$$\mathbf{P}_1 = P_1 \wedge \text{Admin}(P_1) \wedge \text{Compat}(P_1, \text{App}_1)$$

$$\mathbf{P}_2 = P_2 \wedge \text{Admin}(P_2) \wedge \text{Compat}(P_2, \text{App}_2)$$

Let $\text{CS}(\mathbf{P}_i) = P_i$, if $\text{Admin}(P_i) \wedge \text{Compat}(P_i, \text{App}_i)$ is True;
 \emptyset , otherwise.

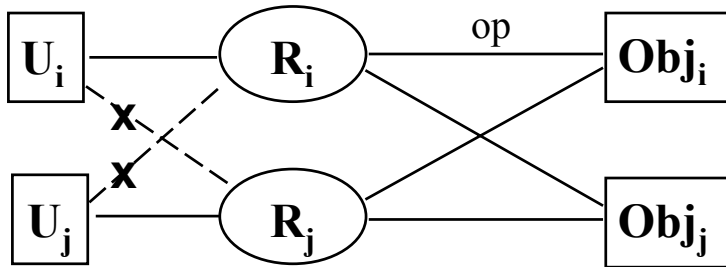
$$\begin{aligned} & \text{(Emerging policy)} \quad \mathbf{P}_1 \circ \mathbf{P}_2 = \\ & = P_1 \wedge P_2 \wedge \text{Admin}(P_1 \wedge P_2) \wedge \text{Compat}(P_1 \wedge P_2, \text{App}_1 \cup \text{App}_2) \end{aligned}$$

$\mathbf{P}_1, \mathbf{P}_2$ are composable if and only if

$$\text{CS}(\mathbf{P}_1 \circ \mathbf{P}_2) \neq \emptyset \text{ whenever } \text{CS}(\mathbf{P}_1), \text{CS}(\mathbf{P}_2) \neq \emptyset$$

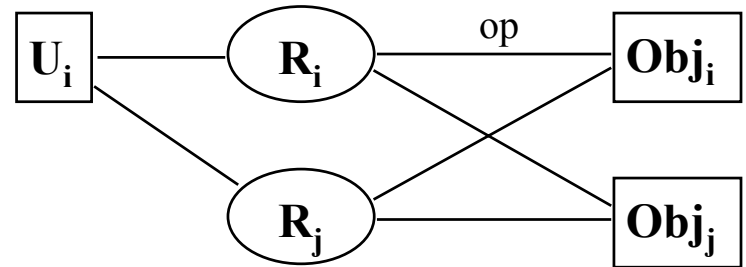
SoD Properties (1)

Static SoD

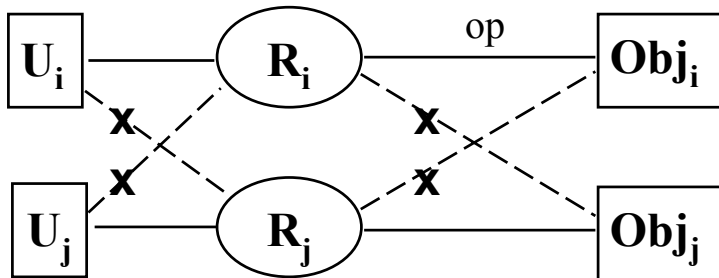


Dynamic SoD

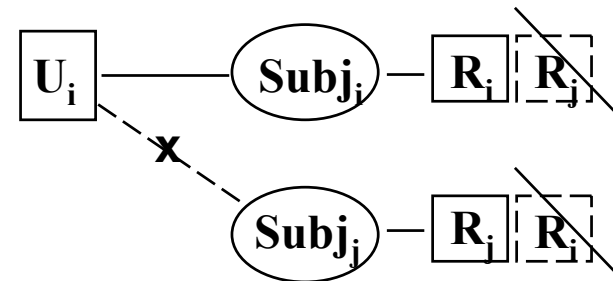
role membership



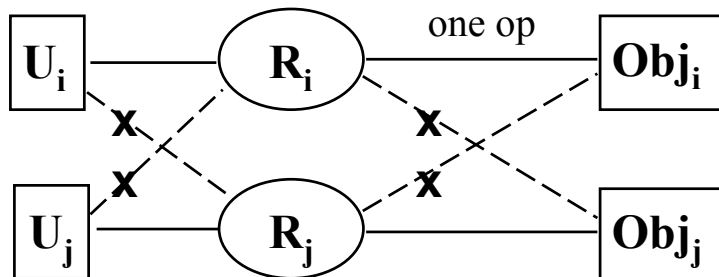
Strict Static SoD



role activation

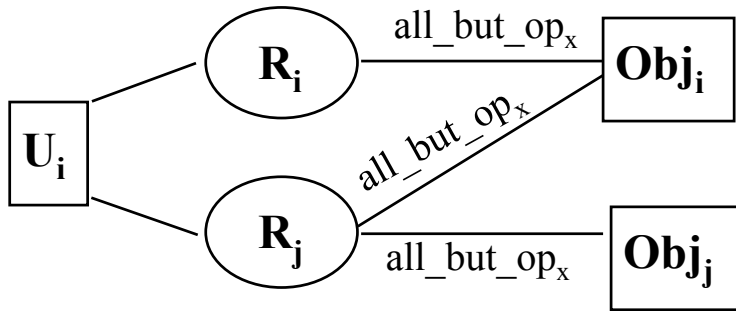


1-step Strict Static SoD

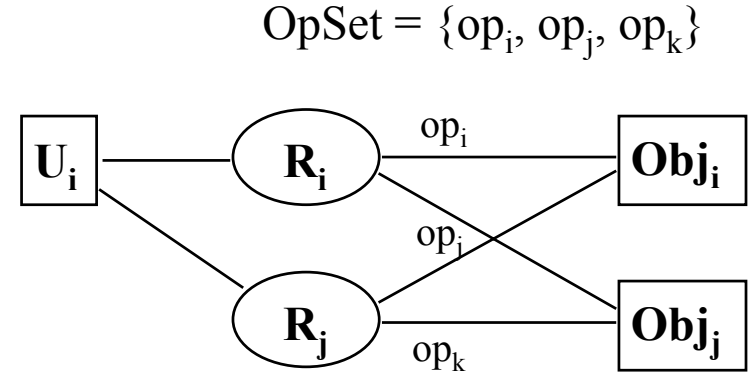


SoD Properties (2)

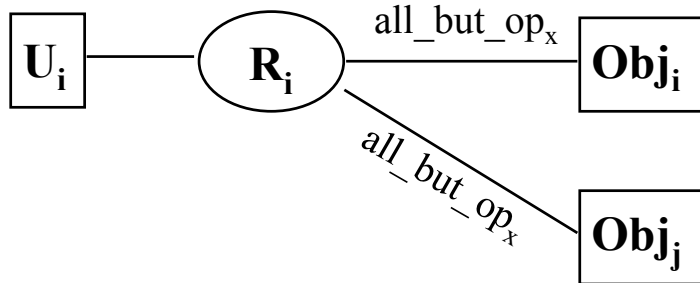
Operational Static SoD



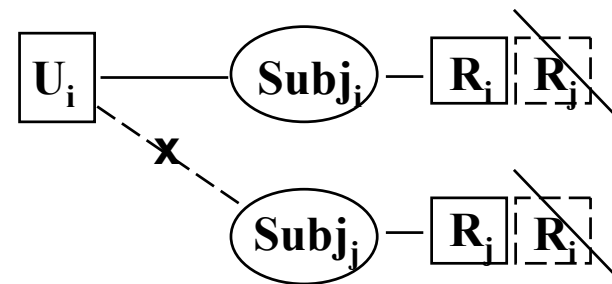
Operational Dynamic SoD



per-Role Operational Static SoD

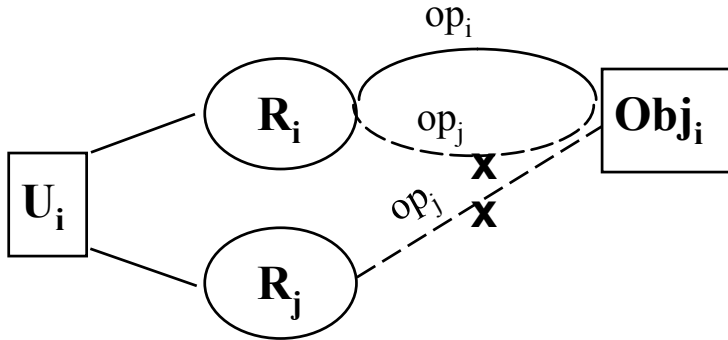


role activation

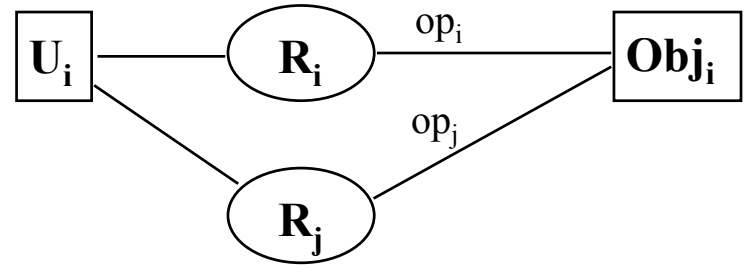


SoD Properties (3)

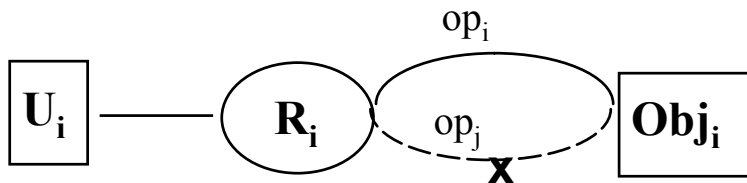
Object-based Static SoD



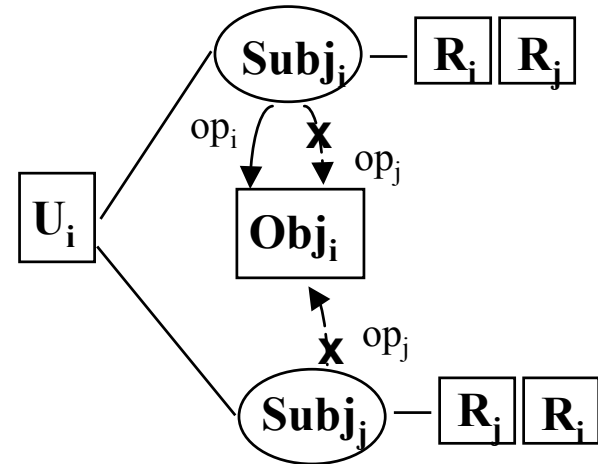
Object-based Dynamic SoD



per-Role, Object-based Static SoD



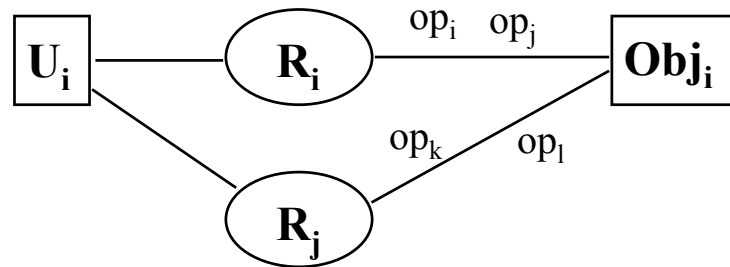
object access



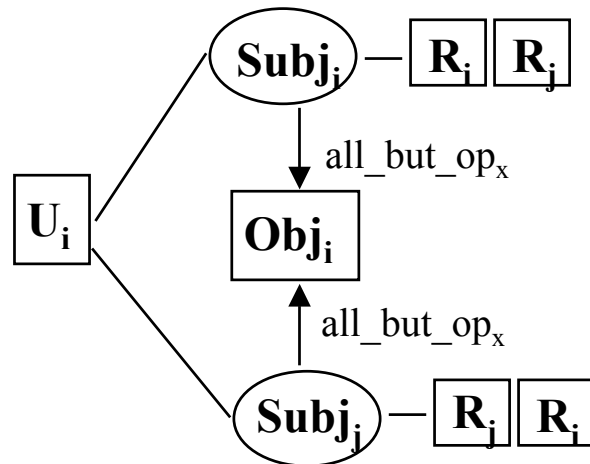
SoD Properties (4)

History-based Dynamic SoD

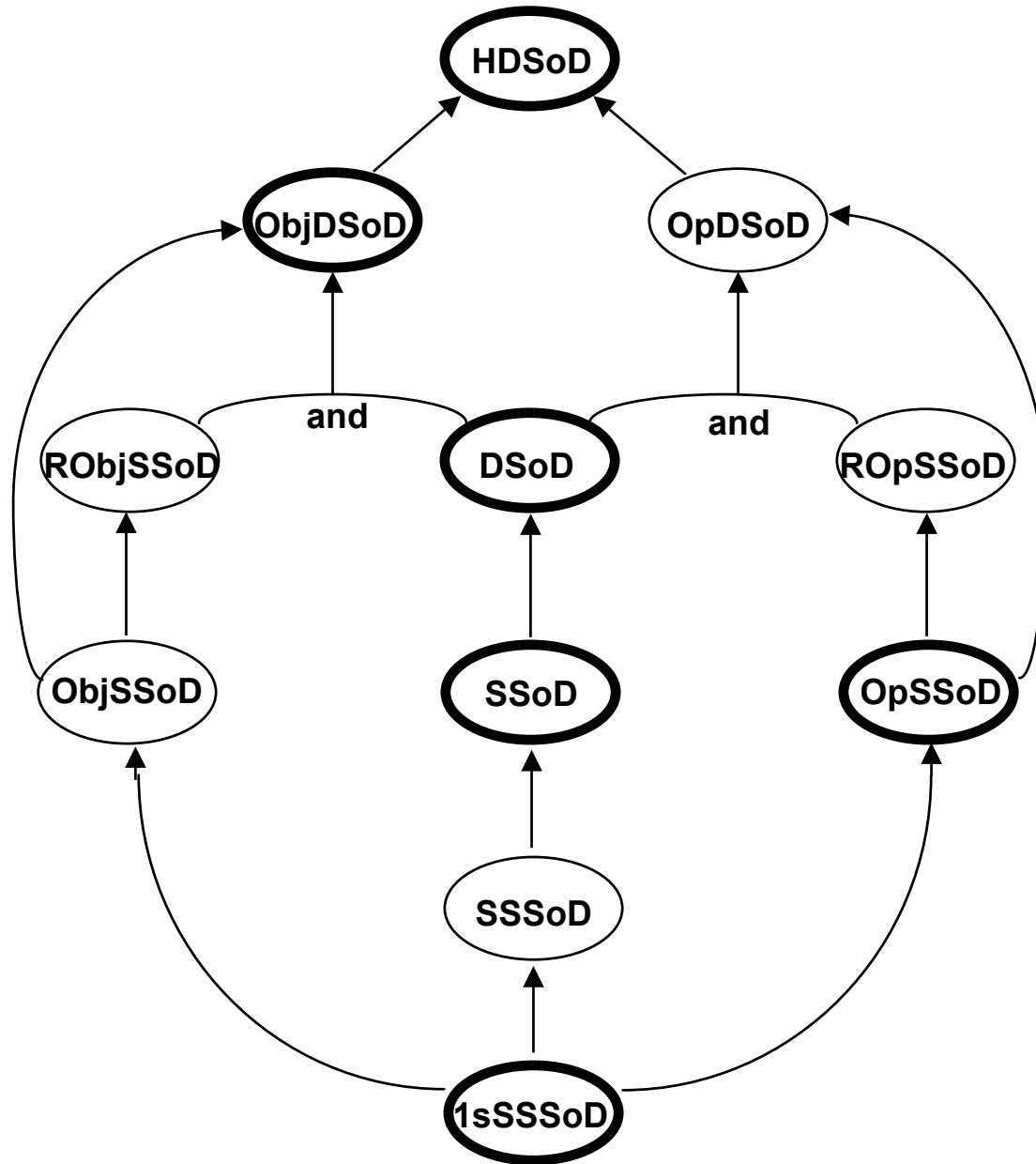
$$\text{OpSet} = \{op_i, op_j, op_k, op_l\}$$



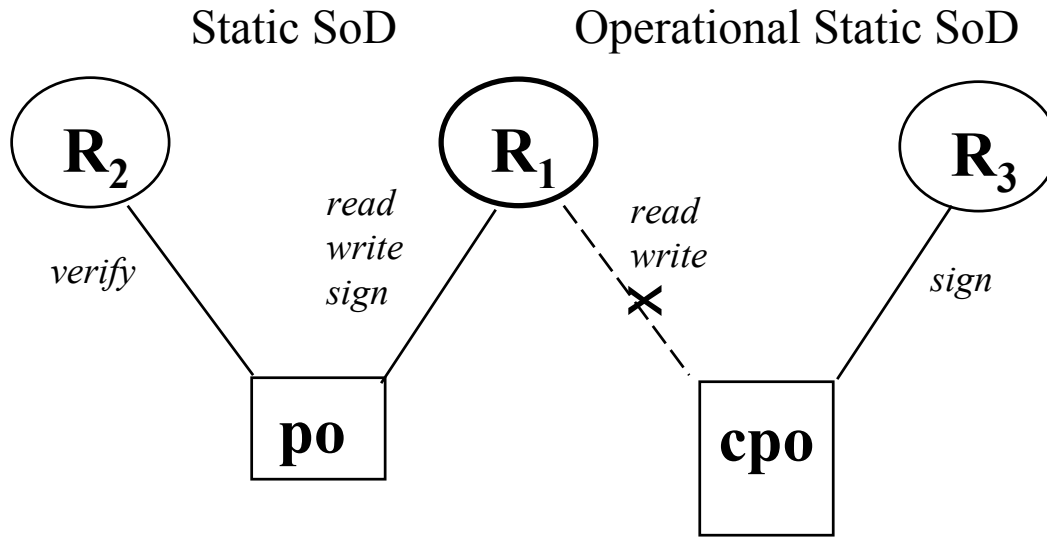
object access



Relationships among SoD Properties

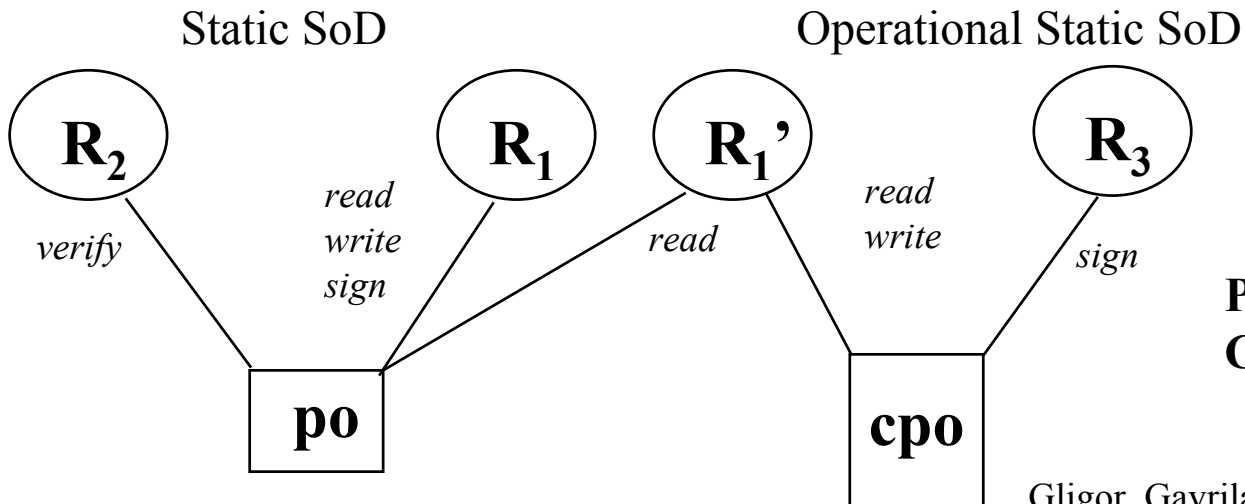


Example: Non-Composable Separation-of-Duty Policies



**Purchasing Staff
Department**

**Purchasing Staff
Central Administration**



**Policy-Management
Change**