

1. Consider the closed loop system

$$\dot{y} = (a - bk)y$$

$$\dot{k} = \beta y^2$$

under assumptions of Lecture Notes 1.

- (i) Solve explicitly this system to obtain  $y(t)$  and  $k(t)$  in analytical form. Write a MATLAB script to plot the results in  $(y, k)$  plane and display the same for a range of initial conditions. (make a reasonable choice of  $a$  and  $b$ )

- (ii) Write a separate ~~MATLAB~~ MATLAB script using a standard numerical integration routine, and check it against your results in (i), for same choice of  $a$  and  $b$  and same initial conditions.

(and hence  $\beta$ )

- (iii) Now allow  $b$  to be time varying by multiplying the choice of  $b$  you made earlier by  $\sin(\omega t)$  for  $\omega = 0.1, \omega = 0.5$

and  $\omega = 0.1$ . Use the numerical method you used in (ii) to integrate closed loop system. Discuss the observed results in these three cases of  $\omega$ .

## 2 READING

Read and understand closely chapters 0 and 1 of the Sasthy-Bodson book upto page 24.